

# Market Structure, Counterparty Risk, and Systemic Risk

Dale W.R. Rosenthal<sup>1</sup>

UIC, Department of Finance

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Four Years After Pittsburgh: OTC Derivatives Reform  
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<sup>1</sup>daler@uic.edu; tigger.uic.edu/~daler

# Counterparty Risk

- *Counterparty*: other side of ongoing financial agreement.
  - A bank enters into a swap with you on the S&P 500.
- Counterparty Risk
  - Risk resulting from default/bankruptcy of a counterparty.
  - Strictly: Risk to you from one of your counterparties.
  - Broadly: Includes effects on overall market (our concern).
- This broad definition we refer to as *systemic risk*.

# Counterparty Risk to Systemic Risk

- Counterparty risk affects market when large failure looms:
  - Near-bankruptcy of Bear Stearns (May 2008)
  - Bankruptcy of Lehman Brothers (Sep 2008)
  - Bankruptcy of Refco Inc? (Oct 2005, owned #1 CME broker)
- Outstanding notional at CME before ceasing trading:

| Bear     | Lehman     | Refco LLC |
|----------|------------|-----------|
| \$761 BB | \$1,150 BB | \$130 BB  |

- N.B. No defaults or trade halts at CME for these events.
- Other bankruptcies: Askin (1994), LTCM (1998, why I care).
- Is counterparty risk an “accelerant” in financial crises?
  - (Yes.) So why couldn't CRWG define counterparty risk?

# Systemic Risk

- Distress increases volatility sharply and significantly.
  - Widens spreads: transactions costs  $\uparrow$ ; market liquidity  $\downarrow$ .
  - Volatility is pushed onto the survivors (externality).
- Crisis bankruptcies have real costs:
  - Virtuous, vicious circles of market and funding liquidity<sup>2</sup>.
  - Reduced funding liquidity affects non-financial firms also.
  - Less invested in risky assets; allocative inefficiency?
  - Higher unemployment: harder job searches, lower tax revenue.
  - Bernanke (1983): affects credit markets; possible depression.

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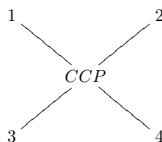
<sup>2</sup>Brunnemeier and Pedersen (2009).

# Results Preview

- Market structure affects contagion and exposure to defaults.
- Specifically: complete networks magnify systemic risk.
  - Disagrees with Allen and Gale (2000), Nier et al (2007).
  - Differing creation of complete networks.
  - Unnetted rehedging lets buyers, sellers create chaos.
- However, cannot eliminate counterparty or systemic risk.
- Tool to estimate market fragility. (not about network genesis)
  - Fragility estimable with a few metrics of market core.
  - Can price distress volatility of differing structures.

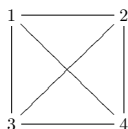
# Model: Market Structures

- Investigate two extremes of  $n$ -counterparty networks.



Star network

(Market with CCP<sup>3</sup>)



Complete network

(Bilateral "OTC" market)

- Each node is a counterparty (capital  $K$ , risk aversion  $\lambda$ ).
- Each edge is a contract<sup>4</sup> linking counterparties  $i$  and  $j$
- Contract exposure:  $q_{ij} = -q_{ji}$ ;  $q_{i < j} \stackrel{iid}{\sim} N(0, \eta^2)$
- Counterparty  $i$ 's net exposure<sup>5</sup>:  $Q_i = \sum_{j \neq i} q_{ij}$ .
- Same net exposures ( $Q_i$ 's) in both networks.

<sup>3</sup>Central counterparty.

<sup>4</sup>A swap or forward on a risky asset.

<sup>5</sup>This is where Diamond & Gale went wrong.

# Model: Event Timing

To study counterparty risk, events occur at discrete times.

$t = 0$ : Bankruptcy of counterparty  $n$  occurs.

- All contracts with counterparty  $n$  are invalidated.
- Pushes unwanted exposure onto other  $n - 1$  counterparties.

$t = 1$ : Living counterparties trade in response to bankruptcy.

$t = 2$ : Living counterparties close out bankruptcy-induced exposure.

Order of trading in a period is random, not strategic.

# Model: Price Impact of Trading

- Each counterparty  $i$  trades shares at times  $t = 1, 2$ .
- Huberman and Stanzl (2004) arbitrage-free price impact.
  - Impact has linear permanent component<sup>6</sup>.
  - Permanent component impacts prices for later traders.
- Trade ordering, price impact create low and high prices.
- Time periods are very short; two simplifying assumptions:
  - ① Prices have no drift other than price impact due to trading.
  - ② Price diffusion is Gaussian (not log-normal).
- Impact would be worse if it reflected counterparty risk fears.

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<sup>6</sup>Price impact could arise from inventory risk cost, non-crisis adverse selection.



# Effects of Invalidated Contracts

- Suppose counterparty A is net long the market.
- $\Rightarrow$  Other counterparties are net short the market.
- These are their preferred equilibrium positions.
- Thus when counterparty A defaults:
  - Survivors must re-create exposure from counterparty A.
  - Survivors become net sellers.
- CCP market: only CCP trades; net sell.
- OTC market: some counterparties will sell, some will buy.
- However, counterparties trade in own interest.
  - Do they re hedge immediately? Push market further?

# Large Bankruptcy

- Consider bankruptcy of a large financial firm.
- Assume large market move  $r_0$  at  $t = 0$  induces bankruptcy.
- Net exposure  $Q_n$  probably large; may estimate via EVT<sup>7</sup>.
  - Trading at  $t = 1, 2$  will move market a lot.
- Move will be further in direction that caused bankruptcy.
- This raises two distressing possibilities:
  - Contagion: move may cause other counterparties to fail; or,
  - Checkmate: hedging may bankrupt the hedger.
- Bilateral OTC: Counterparties anticipate this, trade selfishly.
  - All hedge anticipated follow-on bankruptcy exposure  $\hat{Q}_f$ .
  - Longs, shorts may largely self-segregate re hedge timing.
- Thus network structure matters.

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<sup>7</sup>Equivalent: endow counterparties with perfect information, examine most likely  $Q_n|r_0$ .

# Large Bankruptcy: Equilibrium Trade

- CCP anticipates follow-on bankruptcies  $\Rightarrow$  equilibrium trade.
- OTC traders anticipate one another, follow-on bankruptcies.
  - However: buyers, sellers may separate when they trade.
  - Those same side as net rehedger (most at-risk) rehedger first.
  - Those on other side wait to allow maximum distress.
  - Random trade sequence  $\Rightarrow$  uncertain low price.
  - Use all these to solve for equilibrium OTC net trade.
- In both cases, can estimate two key quantities:
  - Follow-on bankruptcy exposure  $\hat{Q}_f$  (**distress exposure**):
  - # follow-on bankruptcies  $\hat{b}$  (**distress pervasiveness**):

# Strategic Trading: All Together Now?

## Proposition (Pooling)

*In bilateral OTC markets, buyers and seller may split their trades between periods 1 and 2 according to cost minimization. This pooling of buying and selling is a Bayesian Nash equilibrium.*

## Proposition (Separating)

*In bilateral OTC markets, buyers and sellers may separate with buyers in one period and sellers in the other period. This separating of trade timing is a Bayesian Nash equilibrium.*

# Bad Behavior? Checkmate and Hunting

## Proposition (Checkmate)

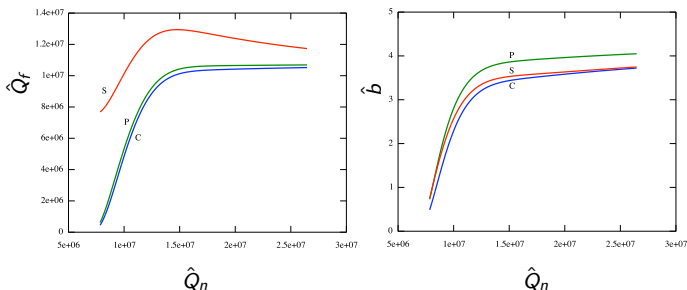
*A large enough initial bankruptcy may yield a follow-on bankruptcy in expectation — despite any finite effort by the troubled counterparty.*

## Proposition (Hunting)

*For a complete network of 3 or more counterparties and a large enough initial bankruptcy, two or more other counterparties may profit by driving a survivor into (follow-on) bankruptcy.*

# Large Bankruptcies: Indicative Distress

- Consider large bankruptcy for  $n = 10$  counterparties<sup>8</sup>.
- Std deviation of bilateral contract exposure  $\eta = 1,000,000$ .
- Distress exposure  $\hat{Q}_f$  and pervasiveness  $\hat{b}$  vs.  $\hat{Q}_n$ .



Lines: (P)ooled OTC; (S)eparated OTC; (C)CP (best case)

$C - P \vee S$ : *Distress envelopes: exposure, pervasiveness* **UIC BUSINESS**

<sup>8</sup>Price impact parameters are as in Almgren and Chriss (2001).

# Large Bankruptcies: From Market Impact to Real Effects

- Suppose  $\hat{Q}_n = \$10$  MM; GARCH variance decay = 0.9.
- For CCP market,  $E(\text{market impact}) = -\$30$ .
  - Effective annual volatility goes from 30% to 38%.
- Pooled OTC buyers,  $E(\text{market impact}) = -\$31$ .
  - Annual volatility  $\uparrow$  to 328% (instant.), 146% (effective).
- OTC buyers, sellers separate:  $E(\text{market impact}) = -\$41$ .
  - Annual volatility  $\uparrow$  to 596% (instant.), 268% (effective).
- \$40 MM mkt size<sup>9</sup>, 8% eq premium, avg risk aversion  $\hat{\lambda} = 3$ .
  - Equilibrium allocation to risky asset: 29% (71% cash).
  - Post-crisis: 19% (CCP), 1.2% (OTC pool), 0.4% (OTC sep).
- Cost of distress externality:
  - \$3.2MM (CCP), \$123 MM (OTC pool), \$425 MM (OTC sep).
  - Cost of OTC market distress is 3–11 $\times$  market size.

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<sup>9</sup>Approximately  $2(\hat{Q}_n + \hat{Q}_f)$ .

# Large Bankruptcies: Not So Random

- Complete networks admit two destabilizing events:
  - Checkmate: weak counterparty may have no beneficial trade.
  - Hunting: counterparties force others into bankruptcy.
- Worse, hunting is a full equilibrium behavior.
  - Market may be pushed far beyond one follow-on bankruptcy.
- Are counterparties selfishly amoral/evil? Maybe not.
  - Trade amount may pre-hedge expected follow-on bankruptcies.
  - This reduces surprise need for trading in period 2.
- CCP markets have fewer such destabilizing events.
  - Suggests central clearing reduces OTC market volatility.
- If traders fear CCP may fail, result here is best case:
  - Result probably lies somewhere inside distress envelope.



# Conclusion

- Even small bankruptcies temporarily increase volatility.
- For a large bankruptcy in a bilateral OTC market:
  - Counterparties may be unable to save themselves (checkmate).
  - Counterparties may hunt their weakest peers for profit.
  - Volatility externality (and thus cost) higher than CCP market.
- Self-segregating buyers, sellers in OTC markets can be nasty:
  - Externality distress cost  $\gg$  market size. (market failure!)
- Suggests benefits to centralized clearing in OTC markets<sup>10</sup>.
- Volatility externality cost  $\Rightarrow$  when to move markets to CCP.
- Three metrics may tell us when markets are more/less brittle.
  - $n$  = # counterparties in market core (complete network);
  - $\bar{K}$  = mean capital for core counterparties; and,
  - $\eta$  = std deviation of core counterparties risk exposure.

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<sup>10</sup>Biais, Heider, Hoerova (2011) suggests CCP is capital efficient.

## P.S. Difference from Allen and Gale (2000)

- Allen and Gale (2000): complete networks are more robust.
- I disagree: complete networks are more fragile.
- Why? Differing methods of network construction.
- Allen and Gale approach: top-down.
  - Net exposure:  $Q_i \stackrel{iid}{\sim} N(0, (n-1)\eta^2)$
  - Contract exposure:  $q_{ij} = Q_i / (n-1)$ . (all same sign)
- My approach: bottom-up.
  - Contract exposure:  $q_{i < j} \stackrel{iid}{\sim} N(0, \eta^2)$ ;  $q_{ij} = -q_{ji}$ ;
  - Net exposure:  $Q_i = \sum_{j \neq i} q_{ij}$ ;  $Q_i \stackrel{iid}{\sim} N(0, (n-1)\eta^2)$ .
- Same net exposures  $Q_i$ 's, different contract exposures  $q_{ij}$ 's.
- Strategic separation of buyers, sellers unlikely in A&G.