

# Transaction Taxes in a Price Maker/Taker Market

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# Introduction

- Regulators recently proposed taxing financial transactions:
- Goals of such a tax:
  - Reduce price volatility
  - Raise large revenue from very small tax
  - Solve problem of “too much” trading?
  - Encourage long-term investing
  - Push *harmful* (?) speculators out of the market
- Arguments claimed against such a tax:
  - Reduces: securities' values, market volume, and liquidity
  - Distorts market (reduces market efficiency)
  - Pushes trade to other venues/countries
- Our goal: study costs and (some) benefits of a tax.

# Results Summary

We find that a transaction tax:

- Widens optimal and effective spreads by  $> 3\times$  the tax;
- Reduces likelihood of trading (*i.e.* volume);
  - $\Rightarrow$  half volume @ 50 bp; double search time.
- $E(\text{quote revenue}) \downarrow 50\%$ , gains from trade  $\downarrow 60\%$  @ 50 bp;
- Lowers volatility slightly if no/few market makers, tax  $< 15$  bp;
- Otherwise: Increases volatility (up to  $3\times$  @ 50 bp);
- Is revenue-optimal for 55–70 bp; (!)
- Deadweight loss suggests no tax is socially optimal; and,
- *Increases* the effects of destabilizing speculators.

More market makers: increased spreads, much lower volatility.

# Thinking on Transactions Taxes

- Tobin (1974): help economies manage FX = political goal.
- Pro: DeFazio, Merkel, Summers and Summers (1989), Stiglitz (1989), ul Haq *et al* (1996), Spahn (2002), Pollin *et al* (2003).
- Con: Friedman (1953), Campbell and Froot (1994), Kupiec (1995,1996), Habermeier and Kirilenko (2001), Forbes (2001).
- Umlauf (1993): Sweden, 1% tax; trading left, volatility  $\searrow$ .

Are transaction taxes like trading fees?

- No: fees often benefit one side; taxes hurt both sides.

# Why Extend Foucault (1999)?

- Traders actively choose price taking versus price making.
  - If tax changes decisions, strategic action is key.
- Why extend? Taxes do not play nicely with Foucault (1999).
  - Traders only have two reservation values,  $v \pm L$
  - $\Rightarrow$  either no effect or eliminates trading.
- Extension allows studying endogenized market phenomena:
  - Traders strategically set bid and ask values;
  - Fail to trade if quotes not appealing to next trader;<sup>1</sup>
  - Differences between quoted and effective spreads;
  - Realized volatility.
- Offers insight into how market quality changes with tax

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<sup>1</sup>More fine-grained than buy vs sell in Foucault (1999).

# Setup

- $v =$  asset value (constant)
- Sequence of iid traders enter market, one per period
- Traders iid; may be market maker w.p.  $\mu$  or investor.
  - Private reservation value:  $v + d_t$  where  $d_t \stackrel{iid}{\sim} F$ .
  - Market maker:  $d_t = 0$ ;
  - Investors:  $d_t \stackrel{iid}{\sim} (0, L^2)$ .
- Market continues w.p.  $\rho \in (0, 1)$  after each period.
- Each trader taxed  $\tau$ /share at position entry+exit.

# Strategic Quoting

Traders choose strategically whether or not to quote a bid and ask.

- Consider traders at time  $t$  (Ilsa),  $t + 1$  (Rick),  $t + 2$  (Sam).
- Price maker/taker model; Rick strategically chooses:
  - Take: Trade against Ilsa's quote, or
  - Make: Quote bid  $v - \delta$  and ask  $v + \beta$  for Sam.
- Rick must also determine his optimal  $\delta$  and  $\beta$ .
- Thus Rick chooses  $\max(R_T, R_Q | d_{t+1})$  where:

$R_T$  = benefit of taking Ilsa's bid/ask

$R_Q | d_{t+1}$  = benefit of quoting optimal bid, ask for Sam

# Taking and Quoting Benefits

- Ilsa is in the same position.
- Denote prior trader's<sup>2</sup> quotes by  $v - \delta_{t-1}$ ,  $v + \beta_{t-1}$ .

$$R_T = \max(-d_t - \delta_{t-1}, d_t - \beta_{t-1}) - 2\tau \quad (1)$$

$$R_Q|d_t = \rho \underbrace{F(-R_Q^{0*} - \delta - 2\tau)}_{P(\text{next trader sells at bid})} (d_t + \delta - 2\tau) + \rho \underbrace{F(-R_Q^{0*} - \beta - 2\tau)}_{P(\text{next trader buys at ask})} (\beta - d_t - 2\tau) \quad (2)$$

$$R_Q^{0*} = \int_{\Omega} R_Q|d_t dF \quad (3)$$

- But we need to know that  $R_Q^{0*}$  exists.

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<sup>2</sup>Ugarte's?

# Characterizing Propositions

We characterize equilibrium by proving a few propositions.

- ① Rick will only want to buy from Ilsa, sell to her, or quote.
- ② If  $d_t > 0$ , the bid-ask quote is shifted higher  $(\beta > \delta)^3$
- ③ Bid-ask spread  $\delta + \beta > 4\tau =$  twice trader's tax.
- ④ For quasi-concave pdf w/support on  $\mathbb{R}$ : equilibrium exists.
- ⑤ For  $F = \Phi$  (Gaussian cdf): unique Markov Perfect equilibrium.

Coming soon: closed form results for uniform distribution.

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<sup>3</sup>And likewise for  $d_t < 0$ .

## Model Setup: Numerical Analysis

Consider a market calibrated to typical characteristics:

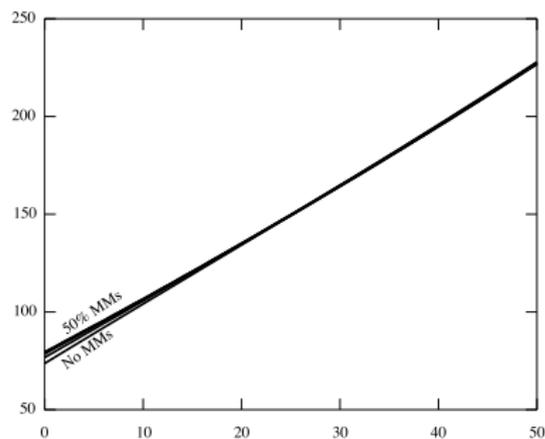
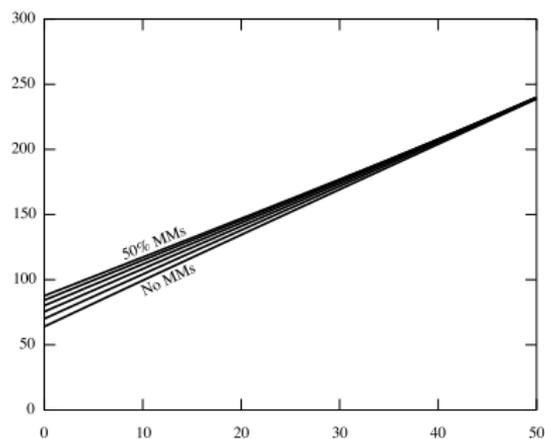
- Value  $v = \$20$ ; private reservation values  $v + d_t$ .
- Traders:  $d_t \stackrel{iid}{\sim} F$
- P(trading continues next period)  $\rho = 0.9$
- Transaction tax  $\tau$ : \$0–\$0.10/share traded (0–50 bp).
- Investor: w.p.  $1 - \mu$ ,  $d_t \stackrel{iid}{\sim} N(0, L^2)$
- Reserve price volatility  $L = \$0.5 = 2.5\%^4$

Some results found via simulation after solving model.

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<sup>4</sup>If daily net trades  $\Rightarrow$  40% annual volatility.

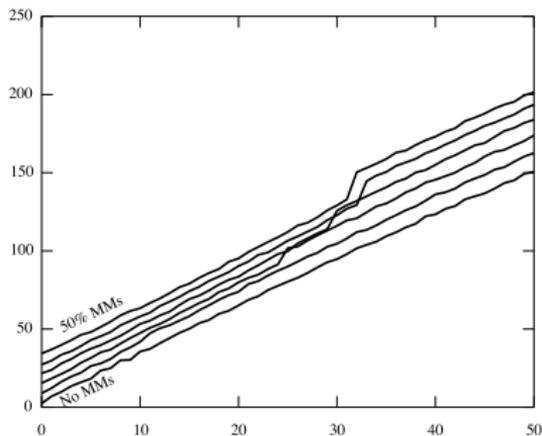
# Optimal (Considered) and Quoted Bid-Ask Spread



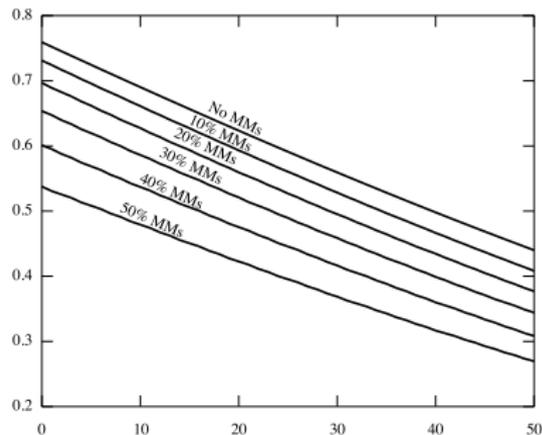
From no tax to 50 bp tax:

- Opt. spread: 60 → 240 bp (no MMs), 85 → 240 bp (50% MMs).
- More MMs = more competition for fill: quoted spread ↑.
- Quoted spreads increase by  $> 3 \times$  tax.
- Quoted spreads are about the same regardless of MMs.

# Effective (Realized) Spread and Fill Rate (Volume)



Effective Spread (bp) vs. tax (bp)

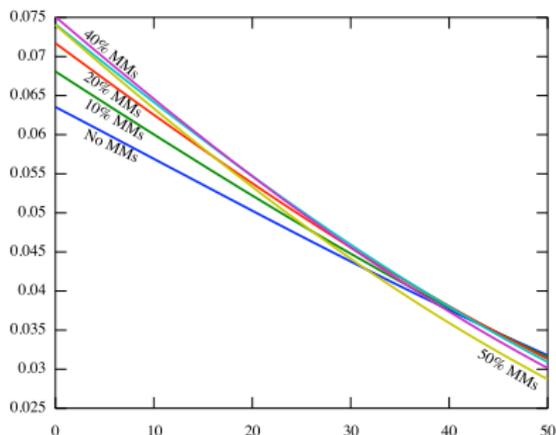


Fill Rate (Volume) vs. tax (bp)

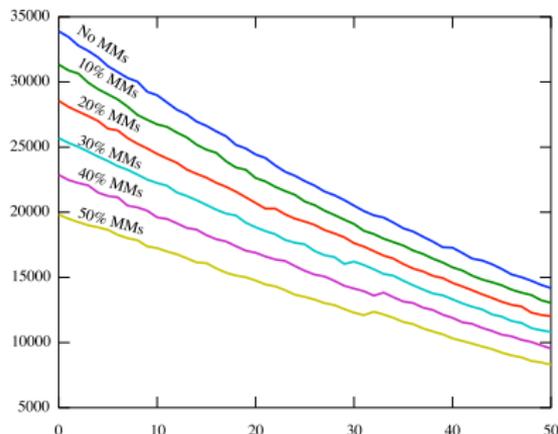
From no tax to 50 bp tax:

- Eff. spread: 0→150bp (no MMs), 40→200 bp (50% MMs).
- More MMs = more competition for fill: effective spread  $\uparrow$ .
- Effective spreads increase by  $> 3\times$  tax.
- Fill rate: 75%→45% (no MMs), 54%→27% (50% MMs)

# Gains from Quoting and Gains from Trade



E(Quoting Benefit)  $R_Q^{0*}$  vs. tax (bp)

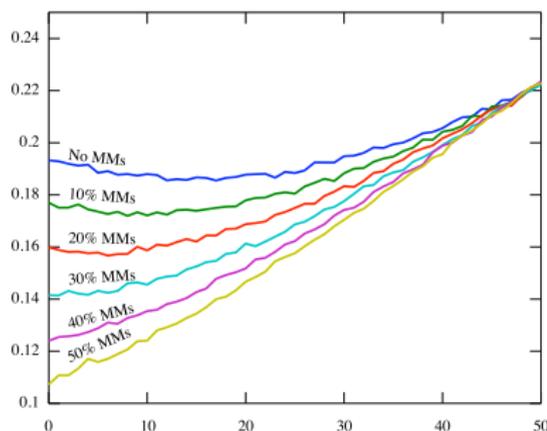


Gains from Trade vs. tax (bp)

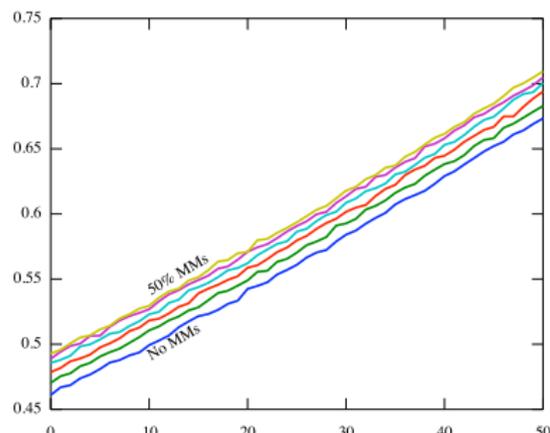
From no tax to 50 bp tax:

- Value of providing liquidity halved.
- Gains from trade decrease by about 60%.

# Volatility and Dispersion of Traders' Reserve Prices



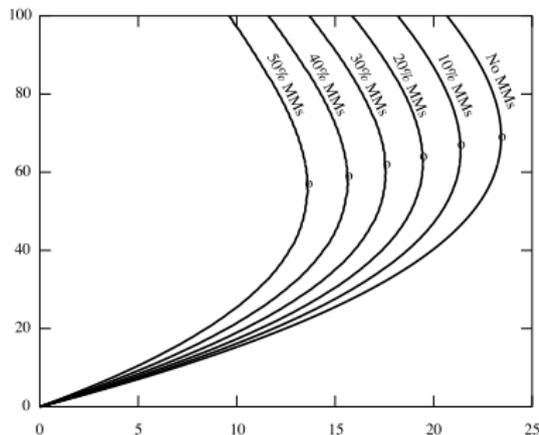
Volatility (\$) vs. tax (bp)



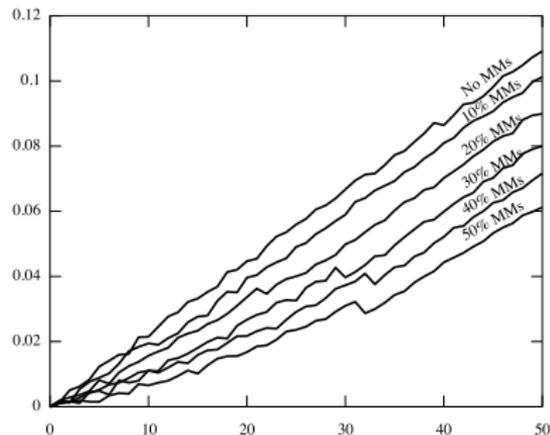
Reserve Price Dispersion (MAD) vs. tax (bp)

- For taxes up to 50 bp, more MMs  $\rightarrow$  lower volatility.
- No MMs: volatility  $\downarrow$  by up to 4% at 15 bp, then increases.
  - Only (weakly) positive benefit but MMs lower volatility more.
- 50% MMs: volatility tripled (!) at 50 bp; most sensitive.
- Taxes *chase away* traders with less extreme views.

# Tax Revenues and Deadweight Loss



Tax (bp) vs. Revenue



Deadweight Loss/Order vs Tax (bp)

- Revenue-optimal tax: 57–69 bp; revenue/order: 14–23 bp.
- More MMs  $\Rightarrow$  lower optimal tax.
- Socially-optimal tax: 0 bp.